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- Note:** **1. PART I** contains explanations and examples of the “puzzle” exercises which are found in Part II.
- 2. PART II** contains practice puzzles, check quizzes, and check tests. These are referenced to the appropriate text pages.

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